

Flow Analysis

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Network Environ Analysis Overview

Systems Ecology
Network Environ Analysis

Pathway Analysis
enumerates number of pathways to travel in a network

Flow Analysis ($g_{ij}=f_{ij}/T_j$)
identifies non-dimensional flow intensities along indirect pathways

Storage Analysis ($c_{ij}=f_{ij}/x_j$)
identifies non-dimensional storage intensities along indirect pathways

Utility Analysis ($d_{ij}=(f_{ij}-f_{ji})/T_i$)
identifies non-dimensional utility intensities along indirect pathways

Fath and Patten 1999

Network Representation for Ecosystems

Graph

Matrix

from column to row

$$F = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ f_{21} & 0 & 0 & f_{24} & 0 \\ 0 & f_{23} & 0 & 0 & 0 \\ 0 & f_{42} & f_{43} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$model = \{F, \vec{z}, \vec{y}, X\}$

$$\vec{z} = \begin{bmatrix} z_1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad \vec{y} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{bmatrix} \quad X = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{bmatrix}$$

Network Throughflow Statistics
 T_j = node throughflow
TST = total system throughflow

Model Assumptions

When we make more assumptions about the model/data we can ask more kinds of questions, but these specific analysis become less general

- Edges = energy—matter flow
 - mg N m⁻² yr⁻¹
 - kcal m⁻² yr⁻¹
- Trace a single thermodynamically conserved tracer
 - e.g. C, N, P, S, energy
- System is at steady state
 - Inputs = outputs

SC Oyster Reef Ecosystem (Dame and Patten 1981)

Throughflow Analysis Algebra

Throughflow Analysis: Summary

Direct Flow Intensity Matrices

output $G_{n \times n} = [g_{ij}] = f_{ij}/T_j$

input $G'_{n \times n} = [g'_{ij}] = f_{ij}/T_i$

Represents the flow intensity from one node to another. Boundary flow driven

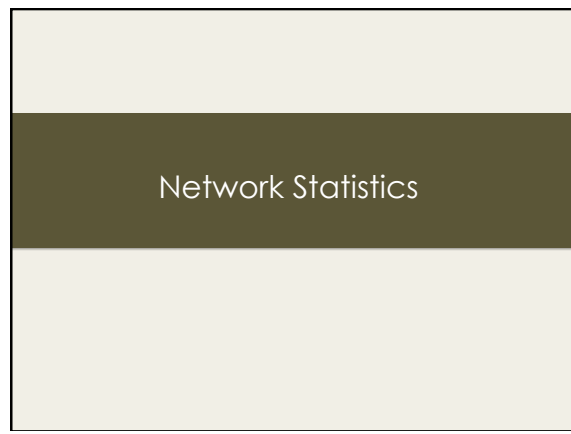
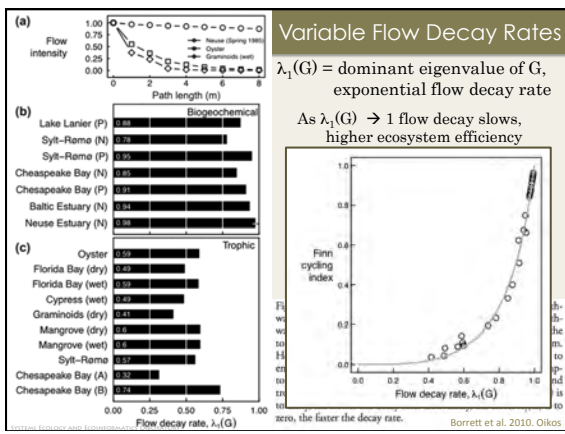
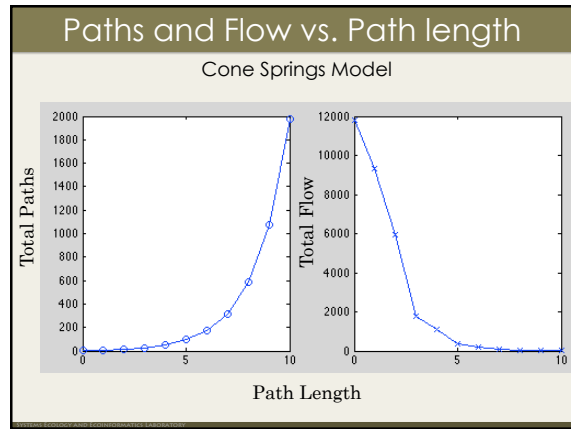
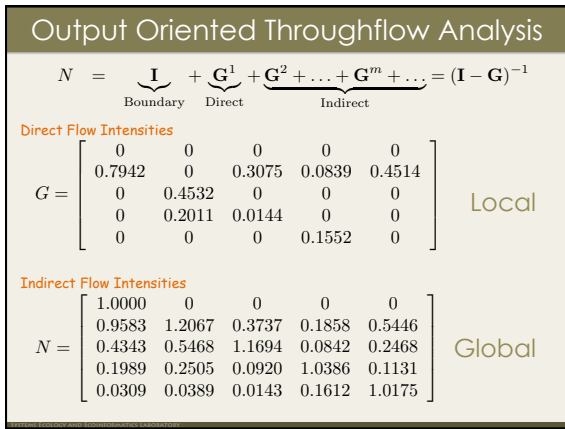
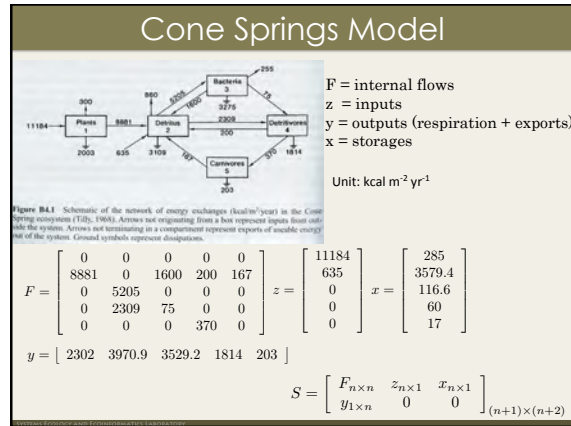
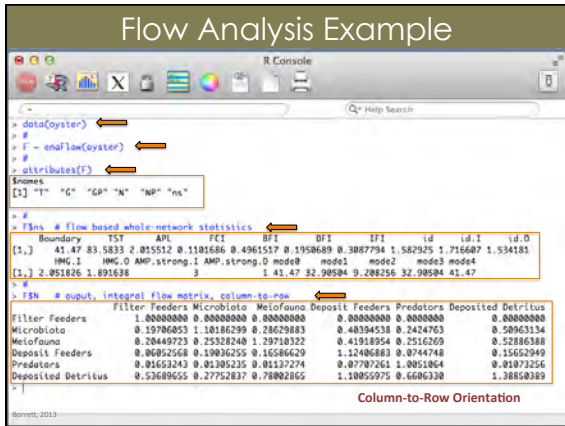
Indirect Flow Intensity Matrices

$$N = \underbrace{I}_{\text{Boundary}} + \underbrace{G^1}_{\text{Direct}} + \underbrace{G^2 + \dots + G^m + \dots}_{\text{Indirect}} = (I - G)^{-1}$$

$$N' = \underbrace{I}_{\text{Boundary}} + \underbrace{G'^1}_{\text{Direct}} + \underbrace{G'^2 + \dots + G'^m + \dots}_{\text{Indirect}} = (I - G')^{-1}$$

Recovering Throughflow

$$\vec{T} = \vec{y}N' \qquad \vec{T} = N\vec{z}$$



Selected Throughflow Statistics

T_j – total amount of stuff flowing into (out of) a node
 TST – sum of T_j
 Indirect/Direct – indicator of importance of indirect flows (effects) [Network non-locality]
 - Multiple ways of calculating – [id, id.i, id.o]

Borrett and Freeze (2011) Ecological Modelling DOI: 10.1016/j.ecolmodel.2010.10.015

TST/Input – network aggradation, average path length, multiplier effect
 Homogenization – a comparison of the evenness of the distribution of flows between a local and a global neighborhood.

```

> # Flow based whole network statistics
Boundary TST AMI FEI BFI BFI BFI id id.i id.o
[1.] 41.47 83.5853 2.855512 0.1181658 0.4961517 0.1952659 0.3887794 1.582325 1.716480 1.534183
HMG_1 HMG_0 AMP_strong.1 AMP_strong.0 mode0 mode1 mode2 mode3 mode4
[1.] 2.951826 1.891638 3 1.41 47 32.98594 9.288256 32.98594 41.47
    
```

NEA Hypotheses: Holoecology

Ecosystem Properties
 Network statistics are indicators

- #8–Network aggradation
- #7–Network mutualism
- #6–Network synergism
- #5–Network unfolding
- #4–Network amplification
- #3–Network homogenization
- #2–Network dominant indirect effects
- #1–Network path proliferation
- [-]–Network integration

...now up to 13
 See Jorgensen 2012 Ch 12

KNOWLEDGE · EDIFICE · OF · HOLOECOLOGY

[-]–Network integration

Nature is unified into a singular, coherent, sociological whole by dominant network indirect effects.

Patten, unpublished

Network Homogenization

Ecological Modelling 221 (2010) 1719–1716.

Contents lists available at ScienceDirect
Ecological Modelling

journal homepage: www.elsevier.com/locate/ecolmodel

Evidence for resource homogenization in 50 trophic ecosystem networks

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Network Homogenization

Oyster Reef Model

Direct Flow Intensities

$$G = (g_{ij}) = f_{ij}/T_j$$

$$G = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.37 \\ 0 & 0.15 & 0 & 0 & 0 & 0.33 \\ 0 & 0.15 & 0.078 & 0 & 0 & 0.029 \\ 0.012 & 0 & 0 & 0.069 & 0 & 0 \\ 0.38 & 0 & 0.50 & 0.76 & 0.48 & 0 \end{bmatrix}$$

Integral Flow Intensities

$$N = (I - G)^{-1}$$

$$N = \begin{bmatrix} 1.0 & 0 & 0 & 0 & 0 & 0 \\ 0.26 & 1.1 & 0.29 & 0.40 & 0.24 & 0.51 \\ 0.20 & 0.26 & 1.3 & 0.42 & 0.25 & 0.53 \\ 0.061 & 0.19 & 0.17 & 1.1 & 0.074 & 0.16 \\ 0.017 & 0.013 & 0.011 & 0.077 & 1.0 & 0.011 \\ 0.54 & 0.28 & 0.78 & 1.1 & 0.66 & 1.4 \end{bmatrix}$$

HMG = $\frac{CV(G)}{CV(N)}$

$$= \frac{2.0195}{1.0676} = 1.8916$$

HMG > 1 implies network homogenization

Dome & Patten 1981

Model Database

Trophically-based Ecosystem Networks

50 models
 35 distinct systems

$4 \leq n \leq 125$
 $0.05 \leq C \leq 0.33$
 $0 \leq FCI \leq 0.51$

Uncertainty Analysis

10,000 perturbed models
 +/- 5% of orig. flows

See Borrett and Salas 2010
 For details

Link to the database: www.ecosystems-lab.org/

Model	Units	n	C	FCI	Source	
Lake Friday	gC m ⁻² yr ⁻¹	4	0.26	0.1	0.30	Rohlf et al. 1979
Lake Ontario	gC m ⁻² yr ⁻¹	8	0.28	0.10	0.30	Rohlf et al. 1979
Lake Michigan	gC m ⁻² yr ⁻¹	5	0.40	1.017	0.40	Rohlf et al. 1979
Marine Lake	gC m ⁻² yr ⁻¹	5	0.32	0.10	0.31	Rohlf et al. 1979
Green Springs	gC m ⁻² yr ⁻¹	5	0.32	0.30	0.03	Blay 1969
Little Bannock	gC m ⁻² yr ⁻¹	5	0.23	0.19	0.03	Blay 1969
Dryden Marsh	gC m ⁻² yr ⁻¹	6	0.23	0.20	0.03	Blay 1969
Kaibito	gC m ⁻² yr ⁻¹	8	0.22	0.20	0.03	Blay 1969
Dryden Bay	gC m ⁻² yr ⁻¹	8	0.22	0.14	0.11	Blay 1969
Brown Estuary	gC m ⁻² yr ⁻¹	9	0.30	2.00	0.14	Blay 1969
Northem Bay	gC m ⁻² yr ⁻¹	12	0.24	1.00	0.27	Blay 1969
Richardson Bay	gC m ⁻² yr ⁻¹	12	0.24	1.00	0.27	Blay 1969
Vibron Estuary	gC m ⁻² yr ⁻¹	13	0.25	4.19	0.24	Blay 1969
Ball Lake	gC m ⁻² yr ⁻¹	15	0.17	1.274	0.13	Blay 1969
Delta Estuary	gC m ⁻² yr ⁻¹	16	0.19	1.010	0.32	Blay 1969
Overberg Estuary	gC m ⁻² yr ⁻¹	16	0.17	1.000	0.47	Blay 1969
Southern Benguela Upwelling	gC m ⁻² yr ⁻¹	16	0.25	1.774	0.19	Blay 1969
Paracas Upwelling	gC m ⁻² yr ⁻¹	16	0.22	3.500	0.04	Blay 1969
Coyah River (central)	gC m ⁻² yr ⁻¹	21	0.19	15.003	0.07	Blay 1969
Coyah River (Upper)	gC m ⁻² yr ⁻¹	21	0.18	12.002	0.09	Blay 1969
Chiriqui Mangroves Lagoon	gC m ⁻² yr ⁻¹	21	0.15	6.010	0.18	Blay 1969
Northem Benguela Upwelling	gC m ⁻² yr ⁻¹	24	0.23	6.008	0.09	Blay 1969
Norway Estuary (early summer 1997)	gC m ⁻² yr ⁻¹	30	0.09	13.020	0.12	Blay 1969
Norway Estuary (late summer 1997)	gC m ⁻² yr ⁻¹	30	0.13	13.020	0.13	Blay 1969
Norway Estuary (early summer 1998)	gC m ⁻² yr ⁻¹	30	0.09	14.020	0.12	Blay 1969
Norway Estuary (late summer 1998)	gC m ⁻² yr ⁻¹	30	0.10	13.021	0.13	Blay 1969
Gulf of Mexico	gC m ⁻² yr ⁻¹	31	0.35	18.382	0.19	Blay 1969
Chiriqui Bay	gC m ⁻² yr ⁻¹	31	0.20	16.300	0.18	Blay 1969
Marikina Estuary	gC m ⁻² yr ⁻¹	32	0.37	17.317	0.19	Blay 1969
Norway Estuary	gC m ⁻² yr ⁻¹	32	0.10	3.017	0.31	Blay 1969
Southern Benguela Right	gC m ⁻² yr ⁻¹	33	0.09	17.997	0.18	Blay 1969
Southern Benguela Right	gC m ⁻² yr ⁻¹	36	0.09	3.227	0.19	Blay 1969
St. Marks Bay, site 1 (Jan)	gC m ⁻² yr ⁻¹	01	0.08	1.318	0.13	Blay 1969
St. Marks Bay, site 1 (Feb)	gC m ⁻² yr ⁻¹	01	0.08	1.291	0.13	Blay 1969
St. Marks Bay, site 2 (Jan)	gC m ⁻² yr ⁻¹	01	0.07	1.383	0.09	Blay 1969
St. Marks Bay, site 2 (Feb)	gC m ⁻² yr ⁻¹	01	0.08	1.281	0.09	Blay 1969
St. Marks Bay, site 3 (Jan)	gC m ⁻² yr ⁻¹	01	0.09	12.891	0.01	Blay 1969
St. Marks Bay, site 4 (Jan)	gC m ⁻² yr ⁻¹	01	0.09	2.850	0.04	Blay 1969
St. Marks Bay, site 5 (Jan)	gC m ⁻² yr ⁻¹	01	0.09	1.305	0.09	Blay 1969
St. Marks Bay, site 6 (Jan)	gC m ⁻² yr ⁻¹	01	0.10	1.305	0.09	Blay 1969
Grasslands (Jan)	gC m ⁻² yr ⁻¹	60	0.16	1.919	0.04	Blay 1969
Grasslands (Feb)	gC m ⁻² yr ⁻¹	60	0.16	7.502	0.04	Blay 1969
Ogipasa (Jan)	gC m ⁻² yr ⁻¹	60	0.12	2.972	0.04	Blay 1969
Ogipasa (Feb)	gC m ⁻² yr ⁻¹	60	0.12	1.210	0.04	Blay 1969
Lake Ontario (Jan-20)	gC m ⁻² yr ⁻¹	76	0.22	1.600	0.01	Blay 1969
Lake Ontario (Jan-20)	gC m ⁻² yr ⁻¹	76	0.23	1.487	0.01	Blay 1969
Lake Ontario (Jan-20)	gC m ⁻² yr ⁻¹	76	0.22	1.300	0.01	Blay 1969
Lake Ontario (Jan-20)	gC m ⁻² yr ⁻¹	76	0.23	1.300	0.01	Blay 1969
Marathon (Jan)	gC m ⁻² yr ⁻¹	84	0.10	3.272	0.10	Blay 1969
Marathon (Feb)	gC m ⁻² yr ⁻¹	84	0.10	3.268	0.10	Blay 1969
Florida Bay (Jan)	gC m ⁻² yr ⁻¹	123	0.12	2.721	0.14	Blay 1969
Florida Bay (Jan)	gC m ⁻² yr ⁻¹	123	0.13	1.728	0.08	Blay 1969

Generality of Network Homogenization

HMG occurs in all 50 models
 HMG is robust to uncertainty
 Orientation does not change qualitative results

Median = 1.8
 std. dev. = 1.7

Network Homogenization

Borrett and Salas 2010

**Network Non-Locality
Dominance of Indirect Effects**

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Dominance of Indirect Effects

Hypothesis
Indirect flows dominate direct flows in ecosystems

Consequences
change species roles and who controls resources
hidden relationships
example: Alligators & frogs in the Everglades
(Bondavalli & Ulanowicz 1999)

Salas & Borrett 2011

Dominance of Indirect Effects

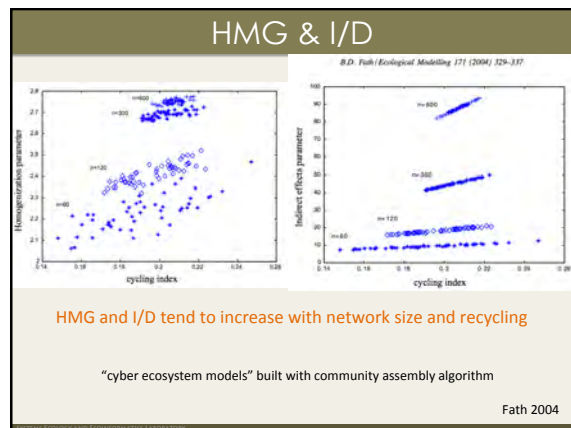
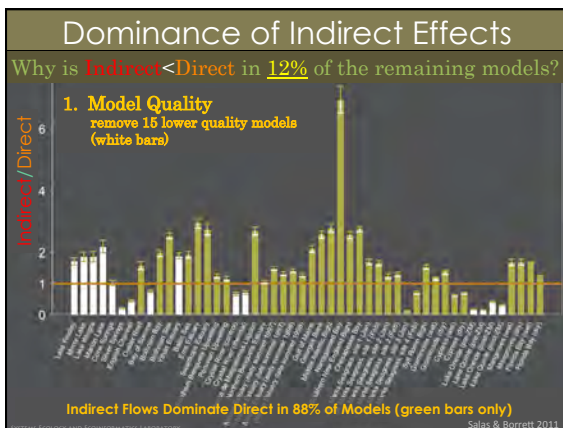
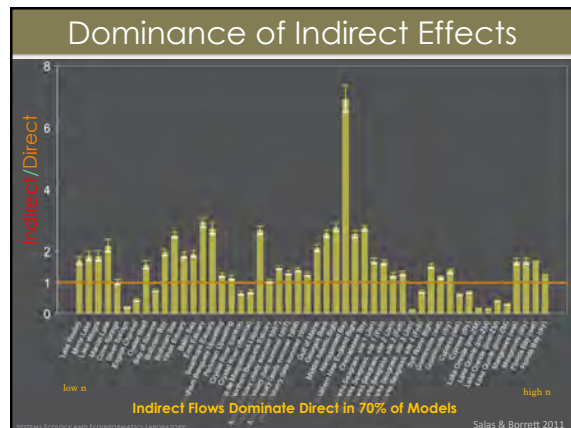
Hypothesis
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Consequences
change species roles and who controls resources
hidden relationships
example: Alligators & frogs in the Everglades
(Bondavalli & Ulanowicz 1999)

Existing Evidence
Oyster Model (Patten 1985)
Algebraic Arguments (Patten and Higashi 1989)
Cyber-Models (Fath 2004)

What about empirically based ecosystem networks?

Salas & Borrett 2011



Other Properties

- Recycling – Finn Cycling Index
- Network Amplification
 - Number of $n_{ij} > 1$ where $i \neq j$
- Network Aggradation
 - $TST/\sum(z_i)$
 - a.k.a. average path length, multiplier effect
 - Consequence of system formation

Throughflow Centrality

Ecological Indicators 32 (2013) 182–196

Contents lists available at ScienceDirect

Ecological Indicators

Journal homepage: www.elsevier.com/locate/ecolind

Throughflow centrality is a global indicator of the functional importance of species in ecosystems

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Borrett, S.R. 2013. *Throughflow centrality is a global indicator of the functional importance of species in ecosystems. Ecological Indicators* 32:182-196
[doi:10.1016/j.ecolind.2013.03.014](https://doi.org/10.1016/j.ecolind.2013.03.014)

What do species do in ecosystems?

John H. Lawton OIKOS 71: 367–374. Copenhagen 1994

- What are the **relative roles** of species/groups in ecosystems and communities?
- Are some species **more or differently** important than another? When? Why? How?
- Describe the **functional roles**

Significance

- Conservation biology and ecosystem management
- Understand biodiversity loss

Rank-Abundance Curves

Two Forest Communities

Relative abundance

Rank abundance

Smith and Smith 2006

Dominant Species

Assume species importance is proportional to its **abundance** or **biomass**

Communities tend to have **few dominants** and a **long tail** of rare species

Whitaker 1965

Diversity of Ecological Importance Concepts

Keystone Species

Importance to Community Structure

Keystone species

Ecosystem Role

Ecological Engineers

Biomass

Foundational Species

Whole Ecosystem Functioning?

Centrality (Social Science)

The relative importance of a node in a network

- **Many** measures with nuanced interpretations
- Often correlated

Importance of indirect flows
(Borgatti 2005, Scotti et al. 2007)

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Proposition

Node Throughflow (T) is a centrality measure

- **Directed** Flow intensities
- **Weighted** Considers all flow over all pathways
- **Global** Captures **internal structure** and **environmental** influence (boundary flows)
- Node importance based on energy-matter flow

1. Evidence to support this claim
2. Demonstrate its utility for characterizing node importance in ecosystem networks

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Throughflow Pathway Decomposition (Output Oriented)

Ecological Network Analysis

$$\vec{T} = (T_j) = \sum_{i=1}^n f_{ij} + y_i$$

Directed & Weighted

Leontief 1936, 1966

$$\vec{T} = \left(\underbrace{G^0}_{\text{boundary}} + \underbrace{G^1}_{\text{direct}} + \underbrace{G^2 + G^3 + \dots + G^m}_{\text{indirect}} + \dots \right) \vec{z}$$

Throughflow is a **globally distributed** property

Captures **system structure & environmental influence**

Centrality indicator of **functional importance**

Hubbell (1965) Status or Centrality

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Throughflow Centrality: Example

Gulf of Maine gww m² yr⁻¹

Is **Throughflow** generally distributed like this in ecosystems?
Few Dominants {PP, DOM, BAC} with long tail

Link et al. 2008

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45 Trophic Ecosystem Models

Model	nodes	edges	FCI	Connectance	T x T ²	FCI ²	Source
Model Database	12	0.22	0.1	0.03	1.1	0.01	Handberg et al. (2006)
Tropically-based Ecosystem Networks	12	0.24	0.17	0.02	1.17	0.02	Handberg et al. (2006)
28 distinct systems	14	0.22	0.17	0.03	1.17	0.02	Handberg et al. (2006)
12 ≤ n ≤ 125	11	0.09	0.04	0.01	0.8	0.00	Handberg et al. (2006)
0.05 ≤ C ≤ 0.37	11	0.09	0.04	0.01	0.8	0.00	Handberg et al. (2006)
0 ≤ FCI ≤ 0.51	11	0.09	0.04	0.01	0.8	0.00	Handberg et al. (2006)

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Example Throughflow Distributions

Bothnian Sea

H₀: even distribution

Chesapeake Bay

Cumulative Throughflow vs Node Rank

N₅₀ {0.08, 0.19, 0.33}

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Throughflow Thresholds

1. More than half of the TST requires 4 or fewer nodes
2. Less than 20% of nodes account for 80% or more of TST
3. As models increase in size the N_{80/n} declines

73% models < 20%

N₅₀ N_{80/n} * 100%

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Demonstration	Model	T ₁	T ₂	T ₃	T ₄
N ₅₀ Dominant Species	Behlman Bay	DICM	Bacteria	Sediment C	Pelagic Producers
	Behlman Sea	Macrobenthos	Pelagic Producers	Sediment C	Pelagic Producers
	Vikar Estuary	Nutrient Pool	Suspended POC	Benthic Macrophytes	
	Southeastern Mangrove (trajinal)	Detritus	Macrophytes	Suspended POC	
	Florida Bay	Pelagic Production	Macrophytes	Suspended POC	
	Ena Estuary	Sediment POC	Pelagic Producers	Benthic Producers	
	Southern Benguela Upwelling	Suspended POC	Macrophytes		
	Peruvian Upwelling	Pelagic Producers	Macrophytes		
	Croftal River (estuarine)	DOC	Detritus		
	Croftal River (fluvial)	Macrophytes	Macrophytes		
	Charra de Magapaloma Lagoon	Sediment POC	Macrophytes	Benthic Deposit Feeders	Cyanobacteria
	Northern Benguela Upwelling	DOC	Bacteria	Bacteria	
	Paratunga Estuary	Sediment POC	Sediment Bacteria		
	Sanjaya Estuary	Sediment POC	Sediment Bacteria	Phytoplankton	
	Kronosek Estuary	Sediment POC	Sediment Bacteria		
	Newau Estuary (early summer 1997)	DOC	Sediment POC	Sediment Bacteria	Sediment Bacteria
	Newau Estuary (late summer 1997)	DOC	DOC	Sediment POC	
	Newau Estuary (early summer 1998)	DOC	DOC	Sediment POC	
	Newau Estuary (late summer 1998)	DOC	DOC	Sediment POC	
	Gulf of Maine	Phytoplankton: Primary	Large Copepods	Detritus POC	
	Georgia Bank	Phytoplankton: Primary	Detritus POC	Bacteria	
	Middle Atlantic Bight	Phytoplankton: Primary	Detritus POC	Bacteria	
	Narragansett Bay	Detritus	Sediment POC	Bacteria	
	Southern New England Bight	Phytoplankton: Primary	Sediment POC	Bacteria	
	Chesapeake Bay	Sediment Particulate Carbon	Bacteria in Sediment POC	Phytoplankton	
	St. Marks Seagrass, site 1 (Jan.)	Benthic Bacteria	Microphytobenthos	Sediment POC	
	St. Marks Seagrass, site 1 (Feb.)	Benthic Bacteria	Sediment POC	Benthic algae	Meiofauna
	St. Marks Seagrass, site 2 (Jan.)	Microphytobenthos	Sediment POC		
	St. Marks Seagrass, site 2 (Feb.)	Sediment POC	Benthic algae	Benthic Bacteria	
	St. Marks Seagrass, site 3 (Jan.)	Microphytobenthos	Sediment POC		
	St. Marks Seagrass, site 4 (Feb.)	Phytoplankton	Sediment POC		
	Hyli Basso Right	Sediment POC	Microphytobenthos	Phytoplankton	
	Grasslands (wet)	Sediment Carbon	Refractory Detritus	Refractory Detritus	
	Grasslands (dry)	Phytoplankton	Sediment Carbon		
	Cypress (wet)	Refractory Det.	Cypress	Living Sediment	Labile Detritus
Cypress (dry)	Refractory Det.	Living sediment	Labile Detritus	Labile Detritus	
Lake Ontario (pre-ZM)	Pelagic Detritus	Diatoms	Blue-green Algae	Ephyrae	
Lake Ontario (post-ZM)	Pelagic Detritus	Diatoms			
Lake Ontario (post-ZM)	Diatoms	Ephyrae			
Lake Ontario (post-ZM)	Diatoms	Zobes-Muscle			
Mangroves (wet)	C in Sediment	Leaf	Other Primary Producers		
Mangroves (dry)	C in Sediment	Leaf	Other Primary Producers		
Florida Bay (wet)	Benthic POC	Water POC	Water Flagellates	Thalassia	
Florida Bay (dry)	Benthic POC	Water POC	Thalassia	DOC	

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	Kronosek Estuary	Sediment POC	Sediment Bacteria		
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	Newau Estuary (late summer 1997)	DOC	DOC	Sediment POC	
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	Narragansett Bay	Detritus	Sediment POC	Bacteria	
	Southern New England Bight	Phytoplankton: Primary	Sediment POC	Bacteria	
	Chesapeake Bay	Sediment Particulate Carbon	Bacteria in Sediment POC	Phytoplankton	
	St. Marks Seagrass, site 1 (Jan.)	Benthic Bacteria	Microphytobenthos	Sediment POC	
	St. Marks Seagrass, site 1 (Feb.)	Benthic Bacteria	Sediment POC	Benthic algae	Meiofauna
	St. Marks Seagrass, site 2 (Jan.)	Microphytobenthos	Sediment POC		
	St. Marks Seagrass, site 2 (Feb.)	Sediment POC	Benthic algae	Benthic Bacteria	
	St. Marks Seagrass, site 3 (Jan.)	Microphytobenthos	Sediment POC		
	St. Marks Seagrass, site 4 (Feb.)	Phytoplankton	Sediment POC		
	Hyli Basso Right	Sediment POC	Microphytobenthos	Phytoplankton	
	Grasslands (wet)	Sediment Carbon	Refractory Detritus	Refractory Detritus	
	Grasslands (dry)	Phytoplankton	Sediment Carbon		
	Cypress (wet)	Refractory Det.	Cypress	Living Sediment	Labile Detritus
Cypress (dry)	Refractory Det.	Living sediment	Labile Detritus	Labile Detritus	
Lake Ontario (pre-ZM)	Pelagic Detritus	Diatoms	Blue-green Algae	Ephyrae	
Lake Ontario (post-ZM)	Pelagic Detritus	Diatoms			
Lake Ontario (post-ZM)	Diatoms	Ephyrae			
Lake Ontario (post-ZM)	Diatoms	Zobes-Muscle			
Mangroves (wet)	C in Sediment	Leaf	Other Primary Producers		
Mangroves (dry)	C in Sediment	Leaf	Other Primary Producers		
Florida Bay (wet)	Benthic POC	Water POC	Water Flagellates	Thalassia	
Florida Bay (dry)	Benthic POC	Water POC	Thalassia	DOC	

Proportion of Models

82 91 40 15

Primary Producers Dead Organic Matter Bacteria Other

Discussion – Ecosystem Organization and Development

- TST → Power (Patten 1991)
 - Operationalized Maximum Power principle (Lotka 1922)
- T_j is partial power
 - Each node is a subsystem, so maximum power should apply to each node
 - Why is throughflow not evenly distributed?
 - restrained by
 - evolutionary constraints of the individual organisms
 - embedded within the existing ecosystem – autocatalysis & centrality

Throughflow Centrality Summary

- Characterizes the relative importance of nodes in an ecosystem network – with respect to flow generation
- Weighted degree type centrality
- Special case of Hubbell Centrality (SNA)
- In ecosystems, TC tends to be concentrated in a few nodes (<4) with a longer tail of less central nodes
- Important nodes tend to be primary producers, detritus, and bacteria

Ecological Network Analysis: Flow Analysis

Flow Analysis Summary

- Introduction to Flow Analysis
- Flow Analysis Algebra
 - main results {T, G, GP, N, NP, ns}
- Network Statistics & Ecosystem Properties
 - Network Homogenization
 - Network Non-locality (dominance of indirect effects)
- Throughflow Centrality
- Ecosystem Impacts of Shrimp Trawling

Suggested Activities

Each Person/Team Should Select a Model
Use enaR to complete the activities

Throughflow Analysis

- Load an example model

```
data(oyster); M=oyster
M=read.scor("filename")
```
- Run throughflow analysis
 - `F = enaFlow(M);`
 - `attributes(F)`
- Investigate Flow network statistics
 - `F$ns`
- Use a for-loop to create a plot of the change in flow intensity, $g_{ij}^{(m)}$, as path length m increases